

Name: \_\_\_\_\_

Instructor: \_\_\_\_\_

**Math 10550, Exam 2**

**October 16, 2014.**

- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for 1 hour and 15 min.
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 10 pages of the test.

|   |     |     |     |     |     |
|---|-----|-----|-----|-----|-----|
| PLEASE MARK YOUR ANSWERS WITH AN X, not a circle! |     |     |     |     |     |
| 1.  | (a) | (b) | (c) | (d) | (e) |
| 2.  | (a) | (b) | (c) | (d) | (e) |
| .....   |     |     |     |     |     |
| 3.  | (a) | (b) | (c) | (d) | (e) |
| 4.  | (a) | (b) | (c) | (d) | (e) |
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| <b>Please do NOT write in this box.</b> |       |
| Multiple Choice                         | _____ |
| 11.                                     | _____ |
| 12.                                     | _____ |
| 13.                                     | _____ |
| 14.                                     | _____ |
| Total                                   | _____ |

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### Multiple Choice

1.(6 pts.) A cylinder has constant height  $h = 2$  m, but the radius is changing. If the volume is increasing at a rate of  $16 \text{ m}^3/\text{sec.}$ , how fast is the radius changing when the radius is 4 m.

- (a) 8 m/sec.                      (b) 1 m/sec.                      (c)  $\frac{1}{\pi}$  m/sec.  
(d) 4 m/sec.                      (e)  $\frac{4}{\pi}$  m/sec.

2.(6 pts.) A beetle is moving along a straight line, with position given by  $s(t) = \sin(t) + \cos(t)$ . How much distance does it travel from  $t = 0$  to  $t = \pi/3$ ?

- (a)  $\frac{\sqrt{3} - 1}{2}$   
(b)  $\sqrt{2} - 1$   
(c)  $2\sqrt{2} - \frac{3}{2} - \frac{\sqrt{3}}{2}$   
(d)  $\frac{\sqrt{3}}{2}$   
(e) None of the above.

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3.(6 pts.) Find the linearization  $L(x)$  of the function  $f(x) = \tan(x)$  at  $\frac{\pi}{4}$ .

(a)  $1 - \frac{\pi}{\sqrt{2}} + \sqrt{2}x$

(b)  $1 - \frac{\pi}{8} + \frac{x}{2}$

(c)  $1 - \frac{\pi}{2} + 2x$

(d)  $1 + \frac{\pi}{2} + 2x$

(e) Does not exist;  $\tan(x)$  is not differentiable at  $\frac{\pi}{4}$

4.(6 pts.) Use linear approximation of  $f(x) = \sqrt{3+x}$  at  $a = 1$  to estimate  $\sqrt{3.6}$ .

(a) 1.9

(b) 1.8

(c) 2.1

(d) 2.2

(e) 3.8

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5.(6 pts.) Consider the function  $f(x) = x^{1/3}(x+1)^2$ . Which of the following is a complete list of the critical points of  $f$ ?

- (a) 1, 1/7, 0                      (b) -1/4, 0, 1                      (c) -1, 0  
(d) 0, -1/7, -1                      (e) -1, -1/7

6.(6 pts.) Let

$$f(\theta) = \frac{\theta^2}{4} + \cos(\theta) \quad \text{where} \quad 0 \leq \theta \leq \pi.$$

Which of the following statements is true about the graph of  $f$ ?

- (a) It is concave up on the interval  $(0, \frac{\pi}{3})$  and concave down on the interval  $(\frac{\pi}{3}, \pi)$ .  
(b) It is concave up on the interval  $(0, \pi)$ .  
(c) It is concave up on the interval  $(\frac{\pi}{3}, \frac{2\pi}{3})$  and concave down on the intervals  $(0, \frac{\pi}{3})$  and  $(\frac{2\pi}{3}, \pi)$ .  
(d) It is concave up on the intervals  $(0, \frac{\pi}{3})$  and  $(\frac{2\pi}{3}, \pi)$  and concave down on the interval  $(\frac{\pi}{3}, \frac{2\pi}{3})$ .  
(e) It is concave up on the interval  $(\frac{\pi}{3}, \pi)$  and concave down on the interval  $(0, \frac{\pi}{3})$ .

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7.(6 pts.) Consider the function  $f(x) = x^3 - 3x^2 - 9x + 2014$ . Which of the following statements is true?

- (a)  $f$  has a local maximum at  $x = -1$ , a local minimum at  $x = 3$ , a point of inflection at  $x = 1$ .
- (b)  $f$  has a local maximum at  $x = 1$ , a local minimum at  $x = -1$ , a point of inflection at  $x = 3$ .
- (c)  $f$  has a local maximum at  $x = 3$ , a local minimum at  $x = -1$ , a point of inflection at  $x = 1$ .
- (d)  $f$  has a local maximum at  $x = -1$ , a local minimum at  $x = 1$ , a point of inflection at  $x = 3$ .
- (e)  $f$  has a local maximum at  $x = 3$ , a local minimum at  $x = 1$ , a point of inflection at  $x = -1$ .

8.(6 pts.) Evaluate  $\lim_{x \rightarrow -\infty} \frac{\sqrt{2x^2 + 1}}{x - 4}$ .

- (a) 2
- (b) -4
- (c)  $\sqrt{2}$
- (d)  $-\sqrt{2}$
- (e) -2

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9.(6 pts.) The **derivative and second derivative** of the function  $f(x)$  are given by

$$f'(x) = \frac{(x-2)(x-3)}{x} \quad \text{and} \quad f''(x) = 1 - \frac{6}{x^2} .$$

On which of the following intervals is  $f(x)$  it both decreasing and concave up?

- (a)  $(\sqrt{6}, 3)$       (b)  $(0, 2)$       (c)  $(-\sqrt{6}, 0)$       (d)  $(3, \infty)$   
(e) It is impossible for a function to be decreasing and concave up on an interval.

10.(6 pts.) What is the minimum value of the function  $f(t) = 2t^3 - 3t^2 - 12t + 6$  on the interval  $[-2, 3]$ ?

- (a) 13      (b) -14      (c) -3      (d) -7      (e) 2

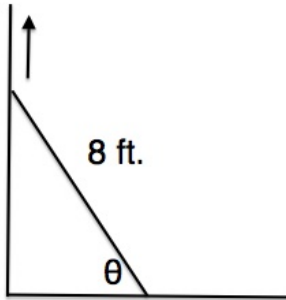
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**Partial Credit**

You must show your work on the partial credit problems to receive credit!

11.(12 pts.) A ladder 8 ft long leans against a vertical wall. The top of the ladder is pulled up from the floor at a rate of 2 ft/second. Let  $\theta$  be the angle between the ladder and the ground. Find  $\frac{d\theta}{dt}$  when the bottom of the ladder is 4 ft away from the wall.



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**12.**(12 pts.) Show that the equation

$$x^7 + 2x^5 + 5x + 4 = 0$$

has one and exactly one real solution. Identify the theorem(s) you are using.



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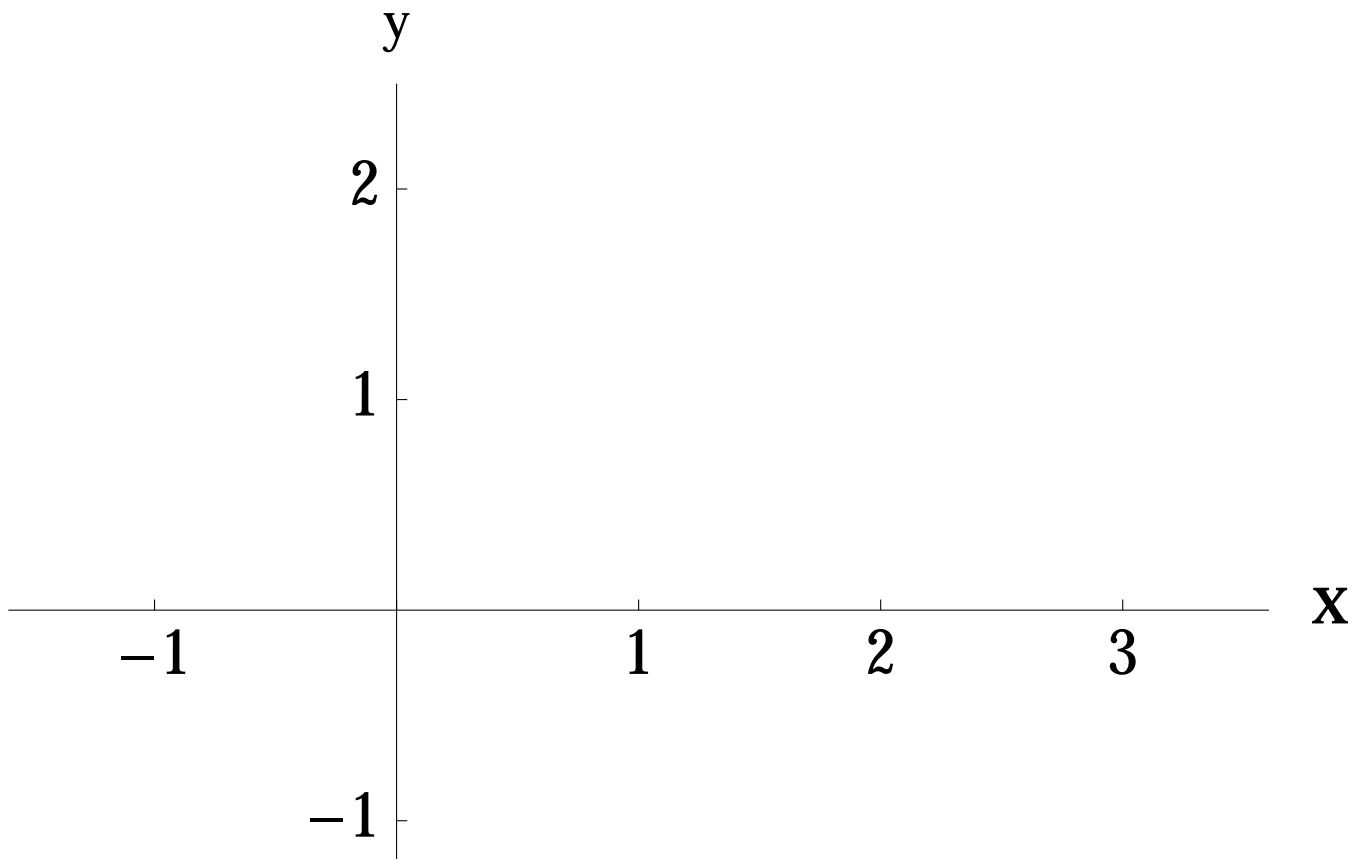
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13.(13 pts.)

The table below shows what is known about a function  $f$  which is **defined and continuous** on the interval  $[-1, 3]$ . The table gives the values (or the sign) of  $f$ ,  $f'$  and  $f''$  at the points given (D.N.E indicates that the derivative does not exist at that point) and tells whether  $f'$  and  $f''$  are positive or negative on the intervals given.

| $x$      | -1 | $(-1, 0)$ | 0 | $(0, 1)$ | 1     | $(1, 2)$ | 2             | $(2, 3)$ | 3    |
|----------|----|-----------|---|----------|-------|----------|---------------|----------|------|
| $f(x)$   | 2  |           | 1 |          | 0     |          | 1             |          | -0.5 |
| $f'(x)$  |    | $< 0$     |   | $< 0$    | 0     | $> 0$    | <i>D.N.E.</i> | $< 0$    |      |
| $f''(x)$ |    | $< 0$     |   | $> 0$    | $> 0$ | $> 0$    |               | $> 0$    |      |

Sketch the graph of a function  $f(x)$  satisfying the above data.



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**14.**(3 pts.) You will earn 3 points if your instructor can read your name easily on the front page of the exam and you mark the answer boxes with an X (as opposed to a circle or any other mark).

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